

Please check whether you have got the right question paper.

14 NOV 2019

N.B: 1. Q 1 is compulsory.

2. Attempt any three from remaining

3. Rights indicate full marks.

1. a. If A, B, C are subset of universal set V then prove that $A \times (B \cap C) = (A \times B) \cap (A \times C)$ 05
- b. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is given by $y = 2x + 1$, prove that f is one to one and onto and find f^{-1} 05
- c. Find $L\{(1 + t\bar{e}^t)^3\}$ 05
- d. Check whether the following function Harmonic or not $3x^2 + \sin x + y^2 + 5y + 4$ 05
2. a. Find k if $f(z) = \frac{1}{2} \log(x^2 + y^2) + i \tan^{-1} \frac{ky}{x}$ is analytic 06
- b. Find $L\{\sin 2t\}$ 06
- c. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = x^2 + 2x - 1$
 $g: \mathbb{R} \rightarrow \mathbb{R}$ $g(x) = -4x^2 + 2$ 08
 Find (I) $f \circ (g \circ f)$ (II) $g \circ (f \circ g)$
3. a. Find Bilinear transformation under which $Z=1, -i, -1$ from point $w=i, 0, -i$ 06
- b. If A be the set of non-integers and let R be a relation on $A \times A$ defined by $(a, b) R (c, d)$ if $ad=bc$, then prove that R is an equivalence relation. 06
- c. Find (1) $L\left\{\int_0^t e^{u} \frac{\sin u}{u} du\right\}$ 08
 (2) $L\{(1 + 2t + 3t^2 + t^3)H(t - 2)\}$
4. a. Use convolution theorem and evaluate 06
 $L^{-1}\left\{\frac{(s+5)^2}{(s^2+10s+16)^2}\right\}$
- b. Find transitive closure of following relation defined on $A = \{a, b, c, d, e\}$ by Warshal algorithm $R = \{(a, a) (a, b) (b, c) (c, d) (c, c) (d, e)\}$ 06
- c. A man speaks truth 3 times out of 5 when a die is thrown he states that it gave an ace what is probability that this event has actually happened. 08

5. a. How many four digit numbers can be formed out of the digits 1, 2, 3, 5, 7, 8, 9 if no digit is repeated twice? How many of them will be greater than 3000. 06
- b. Solve using Laplace transform 06
 $\frac{d^2y}{dt^2} + 9y = 18$ given that $y(0) = 0$ and $y\left(\frac{\pi}{2}\right) = 0$ 08
- c. Evaluate (1) $L^{-1}\left\{\frac{1}{\sqrt{2s+1}}\right\}$ 08
 (2) $L^{-1}\left\{\frac{2s^2-6s+5}{s^3-6s^2+11s-6}\right\}$
6. a. Solve $a_n = 5a_{n-1} - 6a_{n-2}$ for $n \geq 2, a_0 = 0, a_1 = 1$ 06
- b. Find orthogonal curves of family of curves $e^{-x} \cos y + xy = \alpha$, where α is the real constant 06
- c. i. Find the image of rectangular region bounded by $x=0, x=3, y=0, y=2$ under the transformation $w = z + (1+i)$ 08
 ii. A fair dice is thrown thrice. Find probability that sum of numbers obtained is 10.
